

I prefer that you submit your answers on a printed copy of this document, like it's a quiz or exam. However, you may instead rewrite the questions by hand before solving them. Staple sheets together, in order. **Be neat. Always give enough work and clear explanation so that fellow students could follow what you did (from start to finish) just by reading your paper.** Numbers in [ ] give point values for each question.

1. Suppose the position of a particle (as a function of time) is given by  $\mathbf{r}(t) = \langle \cos(\pi t), \sin(\pi t), \sqrt{t} \rangle$ .

[4] (a) Find the velocity, speed and acceleration functions for this particle.

should be  $(-1, 0, 3)$

[4] (b) Find equation(s) which describe the line that's tangent to the graph of  $\mathbf{r}$  at the point  $(0, -1, 3)$ .

[4] (c) Using only your brain, graph the curve  $\mathbf{r}$  for  $0 \leq t \leq 4$ .

**2.** Suppose the position of an object (as a function of time) is given by  $\mathbf{r}(t) = \langle 5 - 3t, t^2, 2 \rangle$ .

[4] (a) Find simplified expressions for the tangential acceleration  $a_T$ , normal acceleration  $a_N$ , and curvature  $\kappa(t)$ .

[4] (b) By hand, find the distance this object travels from  $t = 0$  to  $t = 2$ . You may use this formula:

$$\int \sqrt{a^2 + x^2} \, dx = \frac{x}{2} \sqrt{a^2 + x^2} + \frac{a^2}{2} \ln(x + \sqrt{a^2 + x^2}) + C$$

I want a simplified answer involving  $\ln$  and  $\sqrt{\phantom{x}}$ .