

## ME 2016 Computing Techniques

### Section C - Spring 2017

#### Computing Project One

**Due Thursday, February 16<sup>th</sup> at 3:00pm**

#### Numerical Errors and Root-Finding Algorithms

Please read all instructions (on 2 pages) before starting to write any code.

#### Submission of your answers

- At the end of the class on 02/07, upload any Matlab code that you have written on T-Square
- By 3:00 pm on Thursday 02/16, upload your final Matlab codes on T-Square.
- At the start of the class on 02/16, turn in the print-out of the codes, the print-out of the outputs of your code and the graph.

#### Problem statement

A shock wave, which is an extremely thin non-equilibrium region, is caused by the collision of fast moving gas with slower moving gas (e.g., the leading edge of a supersonic wing). The following equation relates the dimensionless velocity inside the shock wave  $\phi$  to the various parameters of the system:

$$\frac{1 - \phi}{(\phi - \alpha)^\alpha} = \exp[\beta(1 - \alpha)M_1(\xi - \xi_0)]$$

where  $\xi$  is the dimensionless position inside the shock wave,  $M_1$  is the Mach number for the high velocity gas and  $\alpha$  and  $\beta$  are constants. For  $\alpha = 0.32$  and  $M_1 = 2$ , determine  $\phi$  at the leading edge of the shock wave (i.e.  $\xi = \xi_0$ ).

#### Tasks

1. Write the equation to be solved in the form  $f(\phi) = 0$  (for the case  $\xi = \xi_0$ ). Plot the function  $f(\phi)$  as a function of  $\phi$  to get an idea of the value of the root (you can only plot  $f$  for  $\phi > 0.32$ ).
2. Write a function for the *secant* algorithm. The inputs should be the function  $f$  (as an anonymous function handle), the 1<sup>st</sup> initial guess  $x_0$ , the 2<sup>nd</sup> initial guess  $x_1$ , and the maximum allowable approximate percent relative error,  $\varepsilon_a^{max}$ . The outputs of the functions should be the value of the root,  $x_r$ , the value of the approximate percent relative error,  $\varepsilon_\alpha$ , and the number of iterations,  $N_{iter}$ . Name your function *secant*. Verify that your code works by solving Example 6.6 from the textbook.
3. Based on your figure in Question 1, and appropriate values for the initial guesses so that the secant algorithm converges to the true root

4. Using  $\varepsilon_{\alpha}^{max} = 1 \times 10^{-8}\%$  find the value of  $\phi$  using your secant algorithm
5. Verify your answer using the MATLAB  $f_{zero}$  function (use the MATLAB help to figure out the options and syntax for  $f_{zero}$ )
6. Report the value of  $x_r$ ,  $N_{iter}$  and  $\varepsilon_{\alpha}$ .

Submit your codes using a single *m* \_le called *LastnameFirstnameCP1.m* where *Lastname* is your last name and *Firstname* is your first name. This \_le should include two functions: *LastnameFirstnameCP1* and *secant*. The function *LastnameFirstnameCP1* should have no input variables and no output variables. Running the function *LastnameFirstnameCP1* should:

- solve Example 6.6 using the secant algorithm
- print out  $x_r$ , and  $\varepsilon_{\alpha}$  after 3 iterations for example 6.6
- plot the function  $f$
- Solve the equation using  $\varepsilon_{\alpha}^{max} = 1 \times 10^{-8}\%$
- print out  $x_r$ ,  $N_{iter}$  and  $\varepsilon_{\alpha}$ .
- print out  $x_r$  obtained with the  $f_{zero}$  function

Make sure to include comments in your codes as described in class.