

Let's evaluate whether tax revenue can increase with a decrease in the tax rate.

Suppose that individual preferences over consumption (c) and leisure (L) can be represented by a utility.....function

$$u(c, L) = c + 400 \ln L.$$

The hourly wage is \$25 and people have up to 60 hours per week to devote for work hours.

*(a) Derive the expressions for optimal leisure (L), labor supply (l) and consumption (c). What is the optimal number of hours worked and consumption without taxation?*

*(b) The government introduces a linear income tax t that applies to wage. What are the optimal leisure*

*hours (L), labor supply (l), consumption (c), and government revenue R(t)?*

*(c) What is the Laffer Curve equation here? The government is trying to maximize tax revenue. It would*

*like a tax rate of 75%, but officials do not know how to take derivatives and FOC maximization problems to*

*check if this is the revenue maximizing rate.*

*Therefore, they asked you to calculate revenue possibilities and labor supply hours for each of the following*

*tax rates: 5%, 15%, 25%, 35%, 45%, 55%, 65%, 75%. Which tax rate would you recommend to collect maximum revenue?*

*Can you make a rough plot of the Laffer curve for a given tax rate?*

*1 2 Suppose that individual preferences over consumption (c) and leisure (L) take the Cobb-Douglas form*

*instead. Thus,*

$$u(c, L) = c^\alpha L^{1-\alpha}$$

*where  $\alpha = \frac{1}{3}$*

*(d) What is the hours of work (l) function with the tax rate t now?*

*(e) What is the Laffer Curve equation now? Again, calculate revenue possibilities and labor supply hours*

*for each of the following tax rates: 5%, 15%, 25%, 35%, 45%, 55%, 65%, 75%. Which tax rate would you*

*recommend to collect maximum revenue now?*