

# 5.1 | Fundamentals : Sequences, Summations, and Matrices

12  
FEB

  
STATUS

Test in WEEK 3 : INTEGERS AND INDEXED STRUCTURES

1 Given the following sequence:

$$\{a_k\} = 2, 3, 5, 6, 8, 9, \dots \text{ for } k \geq 1$$

**What is  $a_3$ ?**

10 Points

- ☐ 3
- ☐ 5
- ☐ 6
- ☐ k

2 Given the following sequence:

$$\{a_j\} = 1901, 1902, 1903, 1904, 1905, 1906, \dots \text{ for } j \geq 1$$

**What is  $a_{20}$ ?**

10 Points

- ☐ 1919
- ☐ 1920
- ☐ 20
- ☐ 2019
- ☐ No way to figure it out

3 Given the following sequence:

$$\{a_i\} = -8, -4, 0, 4, 8, 12, 16, 20, \dots \text{ for } i \geq 0$$

**What is the location of the term "12"?**

10 Points

- ☐ 12
- ☐ 5
- ☐ 6
- ☐  $i$
- ☐  $a$

**4** Given  $a_n = 4n + 5$ , compute  $a_3$ .

10 Points

- ☐  $a_3 = 17$
- ☐  $a_3 = 3$
- ☐  $a_3 = 9$
- ☐  $a_3 = 19$

**5** Given the following sequence: $-10, -7, -4, -1, 2, \dots$ **Identify the common difference.**

10 Points

- ☐ -3
- ☐ 3
- ☐ 5

**6** Given the following sequence: $4, -28, 196, -1372, \dots$ **Identify the common ratio.**

10 Points

- ☐ 9604

- ☐  $-\frac{1}{7}$
  - ☐  $\frac{1}{7}$
  - ☐  $-7$
  - ☐  $7$
- 

**7** Given  $a_n = 2 \cdot (-3)^n$

**Compute  $a_1$**

10 Points

- ☐ 2
  - ☐ -6
  - ☐ -12
  - ☐ 1
- 

**8** Given:  $a_n = 3a_{n-1} + 1$  and  $a_0 = 2$

**Compute  $a_2$**

10 Points

- ☐  $a_2 = 6$
  - ☐  $a_2 = 7$
  - ☐  $a_2 = 22$
  - ☐  $a_2 = 21$
- 

**9** Given:  $a_n = n^{n+1}$

**Compute  $a_3$**

10 Points

- ☐ 28
- ☐ 81
- ☐ 16
- ☐ 27

**10** Given the recurrence relation  $a_n = -2a_{n-1}$  where  $a_0 = -1$ , find  $a_5$

10 Points

- ☐ -64
- ☐ -16
- ☐ -4
- ☐ 32

**11** Given the recurrence relation  $a_n = a_{n-1} - a_{n-2}$  where  $a_0 = 2$ ,  $a_1 = 0$ , find  $a_5$

10 Points

- ☐ 2
- ☐ 0
- ☐ -3
- ☐ 4

**12** Given the recurrence relation  $a_n = 3(a_{n-1})^2$  where  $a_0 = 1$ , find  $a_3$ .

10 Points

- ☐ 3
- ☐ 27
- ☐ 14348907
- ☐ 2187

**13** Given the recurrence relation:  $a_n = 3a_{n-1}$  with initial condition  $a_0 = 2$

**Find the closed form of  $\{a_n\}$**

10 Points

- ☐  $a_n = 2n + 3$
- ☐  $a_n = 2 \cdot 3^n$
- ☐  $a_n = 3 \cdot 2^n$

☐  $a_n = 3n + 2$

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**14**

Given the recurrence relation:  $a_n = a_{n-1} + 2$ , where  $a_0 = 3$ ,

**Find the closed form of  $\{a_n\}$ .**

10 Points

☐  $a_n = 2n + 3$

☐  $a_n = 3n + 2$

☐  $a_n = 2(3)^n$

☐  $a_n = 3(2)^n$

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**15**

Compute the sum:

$$\sum_{k=1}^7 (k + 1)$$

10 Points

☐ 27

☐ 28

☐ 35

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**16**

Compute the sum:

$$\sum_{k=1}^9 (3k - 2)$$

10 Points

☐ 9

☐ 25

☐ 117

☐ 96

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**17**

Compute the sum:

$$\sum_{i=0}^{10} 3$$

10 Points

- ☐  $\sum_{i=0}^{10} 3 = 30$
- ☐  $\sum_{i=0}^{10} 3 = 33$
- ☐  $\sum_{i=0}^{10} 3 = 3$
- ☐  $\sum_{i=0}^{10} 3 = 0$

**18**Given the following sequence  $\{a_k\} = 1, 4, 7, 10, 13, 16, 19, 22, 25, 28, 31, \dots$  starting at  $a_0 = 1$ **Calculate the following sum:**

$$\sum_{i=1}^8 a_i$$

10 Points

- ☐ 92
- ☐ 117
- ☐ 145
- ☐ 175
- ☐ 36

**19**

Compute the sum:

$$\sum_{i=1}^3 \sum_{j=0}^2 i + j$$

10 Points

- ☐ 21
- ☐ 27
- ☐ 3

**20** Which formula gives the result for

$$\sum_{i=1}^n i$$

10 Points

- ☐  $n^2 + n + 1$
- ☐  $\frac{n^3 - n^2}{2}$
- ☐  $\frac{n^2 + n + 1}{2}$
- ☐  $\frac{n^2 + n}{2}$

**21** Let

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \\ 13 & 14 & 15 \end{bmatrix}$$

**How many columns does A have?**

10 Points

- ☐ 2
- ☐ 3
- ☐ 4
- ☐ 5

**22** Let

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \\ 13 & 14 & 15 \end{bmatrix}$$

**How many rows does A have?**

10 Points

- ☐ 2
- ☐ 3
- ☐ 4
- ☐ 5

**23**

Let

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \\ 13 & 14 & 15 \end{bmatrix}$$

**What size is A?**

10 Points

- ☐ 3x5
- ☐ 15
- ☐ 5x3

**24**

Let



$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \\ 13 & 14 & 15 \end{bmatrix}$$

**What is the second row of A?**

10 Points

- ☐  $\begin{bmatrix} 2 \\ 5 \\ 8 \\ 11 \\ 14 \end{bmatrix}$
- ☐  $[4 \ 5 \ 6]$
- ☐  $[13 \ 14 \ 15]$

**25**

Let

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \\ 13 & 14 & 15 \end{bmatrix}$$

**What is the third column of A?**

10 Points

- ☐  $\begin{bmatrix} 2 \\ 5 \\ 8 \\ 11 \\ 14 \end{bmatrix}$
- ☐  $[7 \ 8 \ 9]$
- ☐  $\begin{bmatrix} 3 \\ 6 \\ 9 \\ 12 \\ 15 \end{bmatrix}$

- 26** Let  $A$  be a  $3 \times 4$  matrix,  $B$  be a  $4 \times 5$  matrix, and  $C$  be a  $4 \times 4$  matrix.
- If the following product is defined, select the size of the result. Otherwise, specify it is undefined.**

$CA$

10 Points

- ☐  $3 \times 4$
- ☐  $3 \times 5$
- ☐  $4 \times 5$
- ☐ Undefined

- 27** Let  $A$  be a  $3 \times 4$  matrix,  $B$  be a  $4 \times 5$  matrix, and  $C$  be a  $4 \times 4$  matrix.

**If the following product is defined, select the size of the result. Otherwise, specify it is undefined.**

$AB$

10 Points

- ☐  $3 \times 4$
- ☐  $3 \times 5$
- ☐  $4 \times 5$
- ☐ Undefined

- 28** Given  $A = \begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & 4 \\ 1 & 3 \end{bmatrix}$

**Compute  $A + B$**

10 Points

- ☐  $A + B = \begin{bmatrix} 2 & 5 \\ 3 & 5 \end{bmatrix}$
- ☐  $A + B = \begin{bmatrix} 2 & 5 \\ 4 & 4 \end{bmatrix}$

☐  $A + B = \begin{bmatrix} 2 & 5 \\ 4 & 5 \end{bmatrix}$

☐  $A + B = \begin{bmatrix} 2 & 1 \\ 4 & 5 \end{bmatrix}$

29

Given  $A = \begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & 4 \\ 1 & 3 \end{bmatrix}$

**Compute  $AB$**

10 Points

☐  $AB = \begin{bmatrix} 0 & 4 \\ 3 & 6 \end{bmatrix}$

☐  $AB = \begin{bmatrix} 12 & 8 \\ 11 & 7 \end{bmatrix}$

☐  $AB = \begin{bmatrix} 1 & 11 \\ 2 & 18 \end{bmatrix}$

☐  $AB = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

30

Let  $A = \begin{bmatrix} 4 & -3 \\ 3 & -1 \\ 0 & -2 \\ -1 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} -1 & 3 & 2 & -2 \\ 0 & -1 & 2 & -3 \end{bmatrix}$

**Calculate the following**

$BA$

10 Points

☐  $\begin{bmatrix} -4 & 9 & 0 & 2 \\ 0 & 1 & -4 & -15 \end{bmatrix}$

☐  $\begin{bmatrix} -4 & 0 \\ 9 & 1 \\ 0 & -4 \\ 2 & -15 \end{bmatrix}$

☐  $\begin{bmatrix} -4 & 15 & 2 & 1 \\ -3 & 10 & 4 & -3 \\ 0 & 2 & -4 & 6 \\ 1 & -8 & 8 & -13 \end{bmatrix}$

☐  $\begin{bmatrix} 7 & -14 \\ 0 & -18 \end{bmatrix}$

☐ Undefined

**Submit**

## Comments

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